Required Syllabus Information – all must be included in the course syllabus

#### **MAT 265**

Course Title: Differential Equations: MA1

Course Credits: 3

Course Description: Explores techniques of problem solving and applications. Topics include first, second, and higher order differential equations, series methods, approximations, systems of differential equations, and Laplace transforms.

**GT** Pathways Requirements:

#### **Guaranteed Transfer (GT) Pathways Course Statement:**

The Colorado Commission on Higher Education has approved MA 265 for inclusion in the Guaranteed Transfer (GT) Pathways program in the GT- MA1 category. For transferring students, successful completion with a minimum C- grade guarantees transfer and application of credit in this GT Pathways category. For more information on the GT Pathways program, go to

http://highered.colorado.gov/academics/transfers/gtpathways/curriculum.html.

#### **MATHEMATICS CONTENT CRITERIA GT-MA1**

- a) Demonstrate good problem-solving habits, including:
  - Estimating solutions and recognizing unreasonable results.
  - Considering a variety of approaches to a given problem, and selecting one that is appropriate.
  - Interpreting solutions correctly.
- b) Generate and interpret symbolic, graphical, numerical, and verbal (written or oral) representations of mathematical ideas.
- c) Communicate mathematical ideas in written and/or oral form using appropriate mathematical language, notation, and style.
- d) Apply mathematical concepts, procedures, and techniques appropriate to the course.
- e) Recognize and apply patterns or mathematical structure.
- f) Utilize and integrate appropriate technology.

#### **COMPETENCIES & STUDENT LEARNING OUTCOMES FOR GT-MA1**

#### Quantitative Literacy:

### 1. Interpret Information

a. Explain information presented in mathematical forms (e.g., equations, graphs, diagrams, tables, words).

#### 2. Represent Information

a. Convert information into and between various mathematical forms (e.g., equations, graphs, diagrams, tables, words).

#### 3. Perform Calculations

- a. Solve problems or equations at the appropriate course level.
- b. Use appropriate mathematical notation.

c. Solve a variety of different problem types that involve a multi-step solution and address the validity of the results.

# 4. Apply and Analyze Information

- a. Make use of graphical objects (such as graphs of equations in two or three variables, histograms, scatterplots of bivariate data, geometrical figures, etc.) to supplement a solution to a typical problem at the appropriate level.
- b. Formulate, organize, and articulate solutions to theoretical and application problems at the appropriate course level.
- c. Make judgments based on mathematical analysis appropriate to the course level.

# 5. <u>Communicate Using Mathematical Forms</u>

a. Express mathematical analysis symbolically, graphically, and in written language that clarifies/justifies/summarizes reasoning (may also include oral communication).

## SYSTEM REQUIREMENTS:

## **REQUIRED COURSE LEARNING OUTCOMES**

- 1. Recognize and classify differential equations.
- 2. Use graphical approaches to analyze solution curves.
- 3. Solve first and second order linear, homogeneous and nonhomogeneous differential equations using classical techniques.
- 4. Solve first and second order linear homogeneous and linear nonhomogeneous differential equations using Laplace Transforms and power series.
- 5. Solve 2 by 2 linear homogeneous systems of differential equations.
- 6. Apply differential equations to solve various problems in the physical and natural sciences.

## **REQUIRED TOPICAL OUTLINE**

- I. Recognize and classify differential equations.
  - a. Classification by type
  - b. Classification by order
  - c. Classification by linearity
- II. Use graphical approaches to analyze solution curves.
  - a. Slope fields
  - b. Phase lines
  - c. Phase planes
- I. Solve first and second order linear, homogeneous and nonhomogeneous differential equations using classical techniques.
  - a. Separation of variables
  - b. Integrating factor method
  - c. Method of undetermined coefficients
  - d. Method of variation of parameters
  - e. Methods of substitution such as reduction of order, y over x, etc.
  - f. Exact equations

- g. Auxiliary equations including distinct roots, repeated roots, and imaginary roots
- h. Linear independence
- i. Wronskian Determinants to prove linear independence
- j. Existence and Uniqueness Theorem
- II. Solve first and second order linear homogeneous and linear nonhomogeneous differential equations using Laplace Transforms and power series.
  - a. Laplace transformations of elementary functions
  - b. Laplace transformations of periodic functions and derivatives
  - c. Laplace transformations of inverse transforms
  - d. Power series solutions
  - e. Solve 2 by 2 linear homogeneous systems of differential equations.
  - f. Matrix forms for systems of differential equations
  - g. Distinct real, repeated and complex eigenvalues
- III. Apply differential equations to solve various problems in the physical and natural sciences.
  - a. Spring mass systems
  - b. Growth and decay
  - c. Newton's Law of Cooling

CCCOnline Course Policies: http://www.ccconline.org/ccconline-course-policies/

Effective Implementation date: Spring 2018, 201830