Effective Fall 2018, 201920

Required Syllabus Information - all must be included in the course syllabus

MAT 201 Course Title: Calculus I: MA1 Course Credits: 5

**Course Description:** Introduces single variable calculus and analytic geometry. It includes limits, continuity, derivatives, and applications of derivatives as well as indefinite and definite integrals and some applications.

## **GT Pathways Requirements:**

## **Guaranteed Transfer (GT) Pathways Course Statement:**

The Colorado Commission on Higher Education has approved MAT 201 for inclusion in the Guaranteed Transfer (GT) Pathways program in the GT- MA1 category. For transferring students, successful completion with a minimum C– grade guarantees transfer and application of credit in this GT Pathways category. For more information on the GT Pathways program, go to <a href="http://highered.colorado.gov/academics/transfers/gtpathways/curriculum.html">http://highered.colorado.gov/academics/transfers/gtpathways/curriculum.html</a>.

## **MATHEMATICS CONTENT CRITERIA GT-MA1**

- a) Demonstrate good problem-solving habits, including:
  - Estimating solutions and recognizing unreasonable results.
  - Considering a variety of approaches to a given problem, and selecting one that is appropriate.
  - Interpreting solutions correctly.
- b) Generate and interpret symbolic, graphical, numerical, and verbal (written or oral) representations of mathematical ideas.
- c) Communicate mathematical ideas in written and/or oral form using appropriate mathematical language, notation, and style.
- d) Apply mathematical concepts, procedures, and techniques appropriate to the course.
- e) Recognize and apply patterns or mathematical structure.
- f) Utilize and integrate appropriate technology.

# **COMPETENCIES & STUDENT LEARNING OUTCOMES FOR GT-MA1**

#### **Quantitative Literacy:**

- 1. Interpret Information
  - a. Explain information presented in mathematical forms (e.g., equations, graphs, diagrams, tables, words).

# 2. <u>Represent Information</u>

a. Convert information into and between various mathematical forms (e.g., equations, graphs, diagrams, tables, words).

# 3. Perform Calculations

- a. Solve problems or equations at the appropriate course level.
- b. Use appropriate mathematical notation.

c. Solve a variety of different problem types that involve a multi-step solution and address the validity of the results.

# 4. Apply and Analyze Information

- a. Make use of graphical objects (such as graphs of equations in two or three variables, histograms, scatterplots of bivariate data, geometrical figures, etc.) to supplement a solution to a typical problem at the appropriate level.
- b. Formulate, organize, and articulate solutions to theoretical and application problems at the appropriate course level.
- c. Make judgments based on mathematical analysis appropriate to the course level.

# 5. <u>Communicate Using Mathematical Forms</u>

a. Express mathematical analysis symbolically, graphically, and in written language that clarifies/justifies/summarizes reasoning (may also include oral communication).

# SYSTEM REQUIREMENTS:

# **REQUIRED COURSE LEARNING OUTCOMES**

- 1. Evaluate limits using appropriate analytical, numerical or graphical techniques.
- 2. Analyze the continuity of functions.
- 3. Apply the definition and techniques of differentiation to find derivatives, including derivatives of transcendental functions.
- 4. Analyze functions represented by an equation or a graph using derivatives and limits.
- 5. Create graphs of functions using properties of derivatives and limits.
- 6. Apply techniques of integration to find the antiderivative of a function.
- 7. Evaluate definite integrals using Riemann Sums and the Fundamental Theorem of Calculus.
- 8. Utilize Calculus techniques to solve application problems.

# **REQUIRED TOPICAL OUTLINE**

The required topical outline information MUST be included in the syllabi. It may be incorporated using one of the following variations: copying the topical outline as written below, integrating the topics within the assignment schedule, or listing the topics to be covered.

- I. Limits using appropriate analytical, numerical or graphical techniques
  - a. Limits computation
  - b. Properties of limits
  - c. Limits at infinity
  - d. Infinite limits
- II. Continuity of functions
  - a. Definition of continuity
  - b. Discontinuities with respect to type (removable or non-removable)
  - c. Intermediate Value Theorem
- III. Definition of derivative and techniques of differentiation
  - a. The limit definition of a derivative
  - b. Basic rules of derivatives
  - c. Product Rule
  - d. Quotient Rule
  - e. Chain Rule

- f. Higher order derivatives
- g. Implicit differentiation
- h. Introduction of differentials
- i. Derivatives of trigonometric functions
- j. Derivatives of inverse trigonometric functions
- k. Derivatives of exponential and logarithmic functions
- IV. Functions represented by an equation or a graph using derivatives and limits
  - a. Critical values
  - b. Absolute extrema on an interval
  - c. Increasing and decreasing intervals
  - d. First and Second Derivative Tests for relative extrema
  - e. Inflection points
  - f. Intervals of concavity
  - g. Graphical connection between f and f'
  - h. Asymptotic behavior with limits
  - i. Graphs of functions using properties of derivatives and limits
  - j. Graphing techniques without technology
  - k. Graphing techniques with appropriate technology
- V. Techniques of integration to find the antiderivative of a function
  - a. Indefinite integrals
  - b. Integration by substitution
  - c. Integration of trigonometric functions
  - d. Integration involving inverse trigonometric functions
  - e. Integration involving exponential and logarithmic functions
- VI. Definite integrals using Riemann Sums and the Fundamental Theorem of Calculus.
  - a. Riemann's Sums
  - b. Definite integrals
  - c. Fundamental Theorem of Calculus
  - d. Integration techniques with appropriate technology
- VII. Calculus techniques to solve application problems
  - a. Mean Value Theorem
  - b. Equations of tangent lines
  - c. Related rates
  - d. Rates of change
  - e. Optimization
  - f. Net signed area
  - **g.** Area between two curves

#### **RECOMMENDED TOPICAL OUTLINE**

- I. Additional limit topics
  - a. Verify limits using the limit definition
  - b. Integration and differentiation of additional functions.
  - c. Hyperbolic functions
- II. Additional integration topics
  - a. Numerical integration
  - b. Mean Value Theorem for integrals
  - c. Average Value of a function

- d. Techniques of integration for evaluating functions
- III. Additional applications
  - a. Volumes of revolution using disk and shell methods
  - b. Euler's Method
  - c. Linearization of a function
  - d. Newton's Method
  - e. Physics problems involving work
  - f. Fluid: pressure and force

Syllabi requirements, including legal compliance information must be included. Individual College syllabi guidelines may include additional information. Please contact your VPI/CAO for specific College requirements.